

# Tuesday, August 14, 2012

TISK

- 1) Simplify:  $20 + 3(2^3)$
- 2) Divide. Write your answer in simplest form.  
 $3\frac{2}{3} \div \frac{1}{4}$
- 3) Classify the number  $\sqrt{7}$

We will have 3 mental math questions today.

# Homework Check

18)  $\triangle PMQ \cong \triangle QMN$

20)  $\triangle POQ, \triangle QON, \triangle NOM, \triangle MOP, \triangle QOM, \triangle PON$

22) Sample:  $\overrightarrow{MJ}$  and  $\overrightarrow{MN}$

24) Sample:  $\triangle LMN$

26) No, more than one angle has  $P$  as a vertex, so naming an angle  $\triangle P$  would be confusing.

28) No, both rays contain  $P$  and  $N$ , however, their initial points differ.

29-31) Drawings will vary.

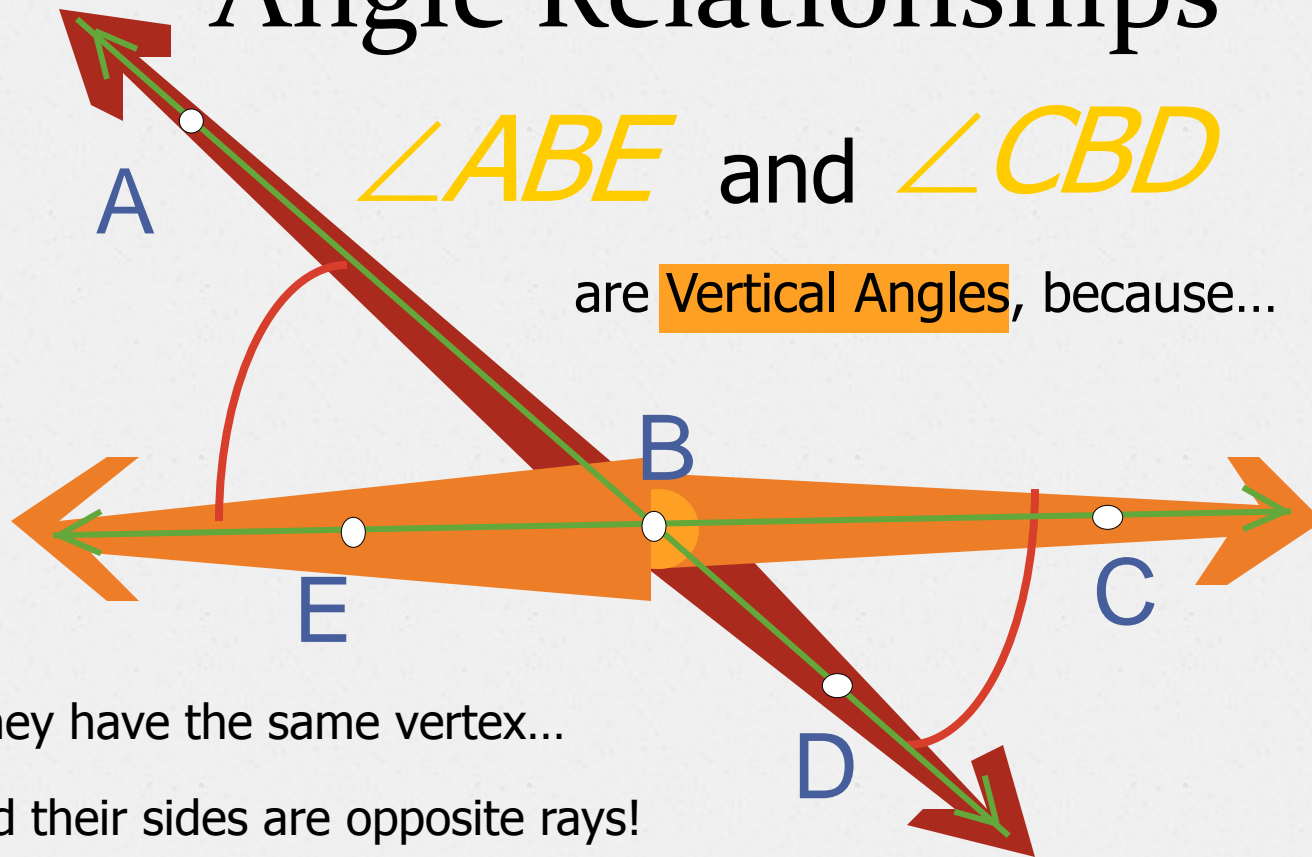
39) a. 1, 3, 6, 10, 15

b. It is an arithmetic sequence.

c. 21, 45

d.  $a = \frac{n(n-1)}{2}$ , where  $a$  = number of angles and  $n$  = number of rays

# Angle Relationships



They have the same vertex...

And their sides are opposite rays!

Can you name another pair of vertical angles in this picture?

# Exploring Vertical Angles

An important **theorem** we will use a lot this year:

## **Vertical Angles Theorem**

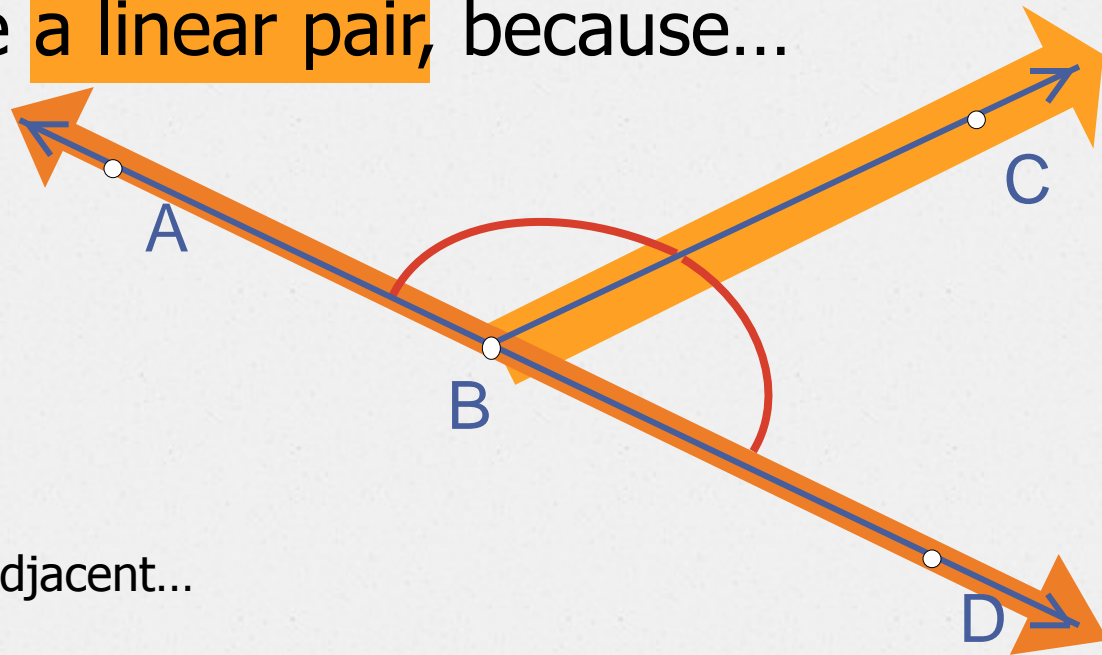
If two angles are vertical angles,  
then they are congruent.

If 2  $\sphericalangle$ s are vertical  $\sphericalangle$ s  $\Rightarrow$  they are  $\cong$

# Angle Relationships

$\angle ABC$  and  $\angle CBD$

are a linear pair, because...



...they are adjacent...

...and their noncommon sides form a line

# Exploring Linear Pairs

An important **postulate** we will use often:

## **Linear Pair Postulate**

If two angles form a linear pair, then the sum of their angle measures is  $180^\circ$ .

If 2  $\sphericalangle$ s are a linear pair  $\Rightarrow$  their sum =  $180^\circ$

# Example 1.

a. Are  $\angle 1$  and  $\angle 2$  a linear pair?

**Yes!**

b. Are  $\angle 4$  and  $\angle 5$  a linear pair?

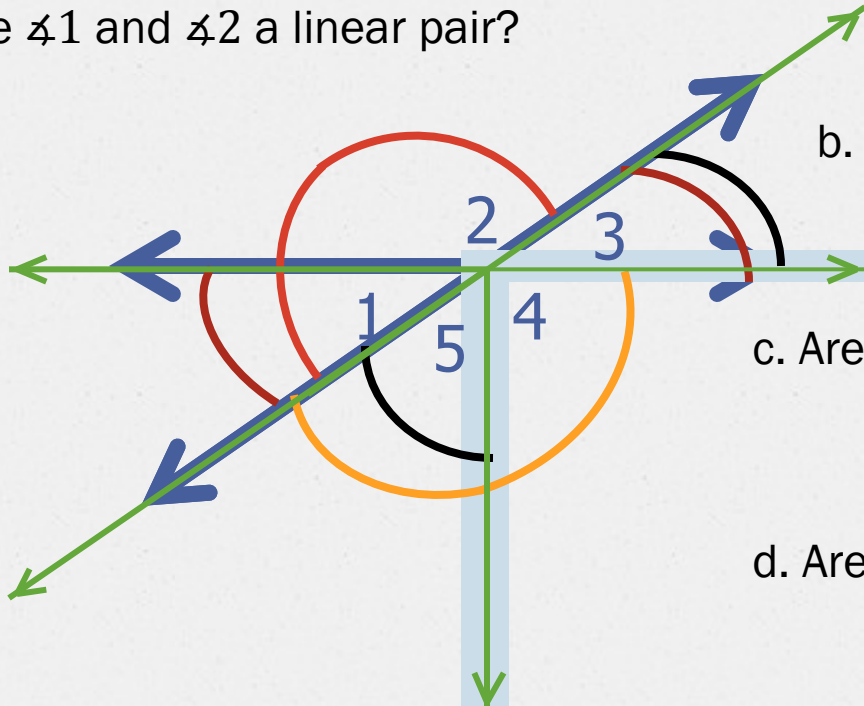
**No!**

c. Are  $\angle 3$  and  $\angle 5$  vertical angles?

**No!**

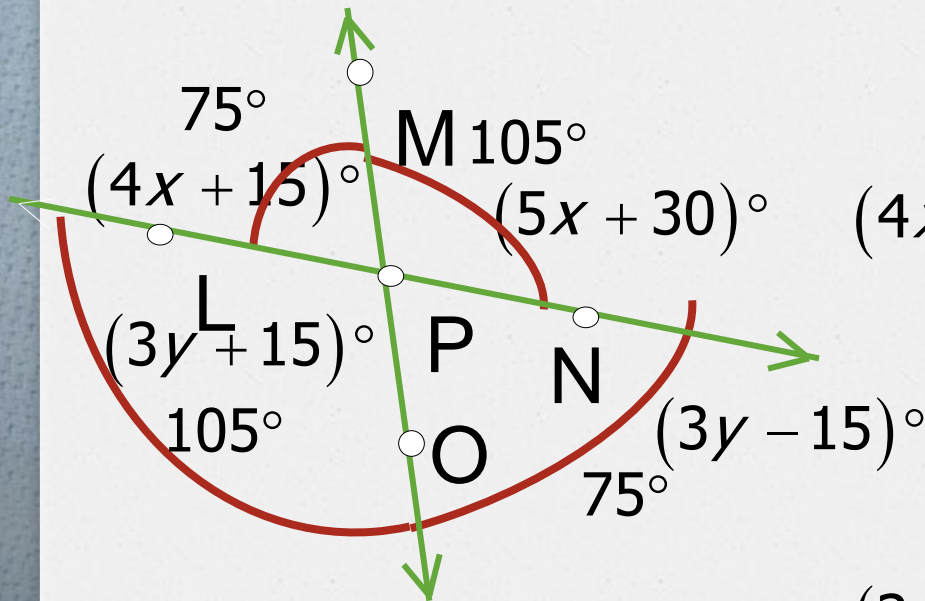
d. Are  $\angle 1$  and  $\angle 3$  vertical angles?

**Yes!**



# Example 2.

o Solve for  $x$  and  $y$ . Then find the angle measures.



$$(4x + 15)^\circ + (5x + 30)^\circ = 180^\circ$$

$$9x + 45 = 180$$

$$9x = 135$$

$$x = 15$$

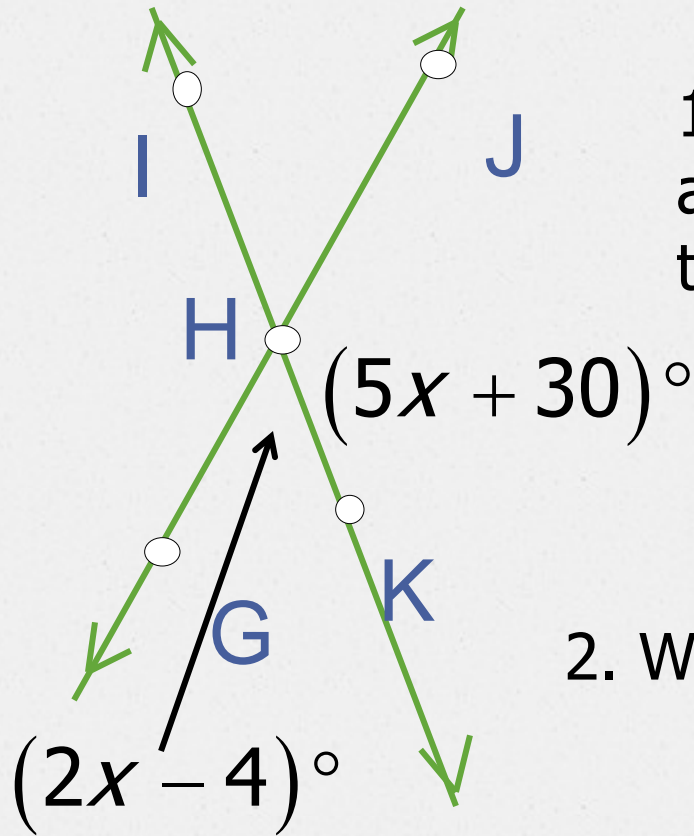
$$(3y + 15)^\circ + (3y - 15)^\circ = 180^\circ$$

$$6y = 180$$

$$y = 30$$



# Check Points!



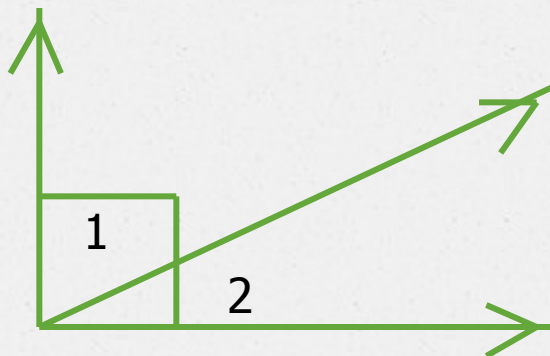
1. Name one pair of vertical angles and one pair of angles that form a linear pair.

2. What is the measure of  $\angle GHI$ ?

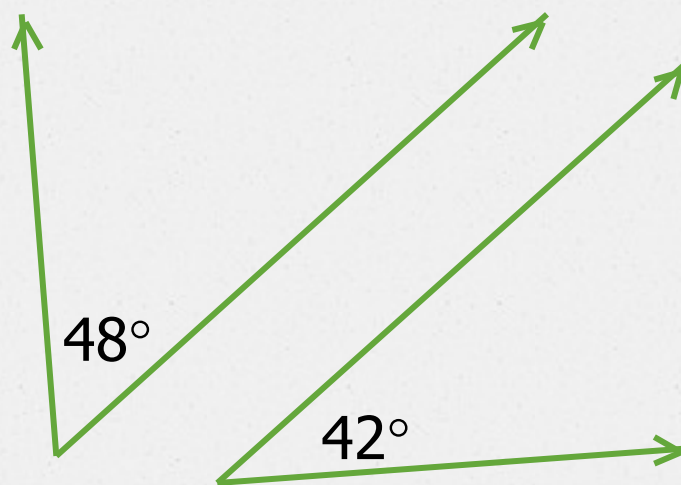
# Angle Relationships

**Complementary Angles** (def.):

Two angles whose measures have a sum of  $90^\circ$ .



complementary,  
adjacent

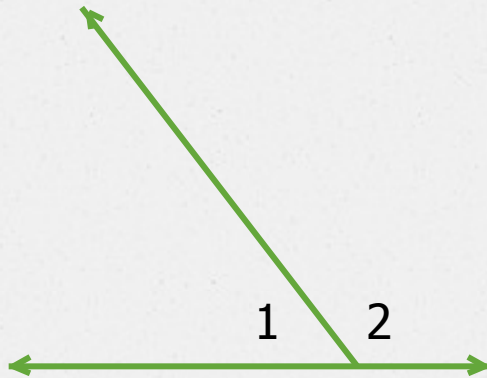


complementary,  
nonadjacent

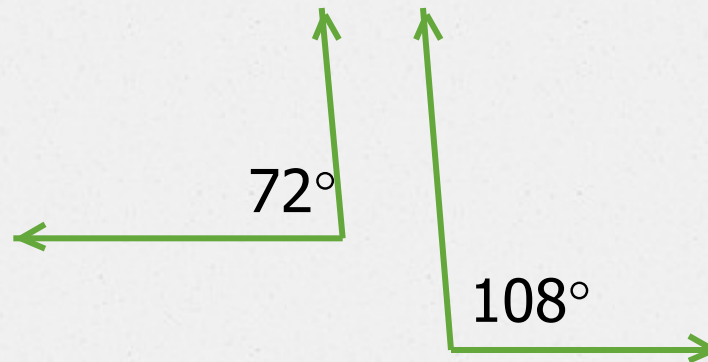
# Angle Relationships

**Supplementary Angles** (def.):

Two angles whose measures have a sum of  $180^\circ$ .



supplementary,  
adjacent



supplementary,  
nonadjacent

## Example 3.

- Given that  $\angle G$  is a supplement of  $\angle H$  and  $m\angle G$  is  $82^\circ$ , find  $m\angle H$ .

$$m\angle G + m\angle H = 180$$

$$82 + m\angle H = 180$$

$$m\angle H = 98$$

- Given that  $\angle U$  is a complement of  $\angle V$  and  $m\angle U$  is  $73^\circ$ , find  $m\angle V$ .

$$m\angle U + m\angle V = 90$$

$$73 + m\angle V = 90$$

$$m\angle V = 17$$

# Example 4.

- $\angle T$  and  $\angle S$  are supplementary. The measure of  $\angle T$  is half the measure of  $\angle S$ . Find  $m\angle S$ .

$$m\angle T + m\angle S = 180$$

$$m\angle T = \frac{1}{2}m\angle S$$

$$\frac{1}{2}m\angle S + m\angle S = 180$$

$$m\angle S + 2m\angle S = 360$$

$$3m\angle S = 360$$

$$m\angle S = 120$$

# Homework

o p. 59 #28-34, 36